

2.5 The Graph of $y = kx^2$

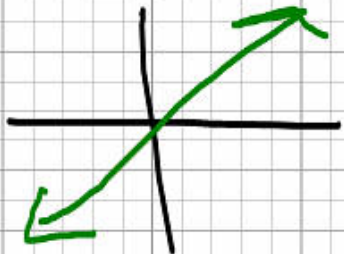
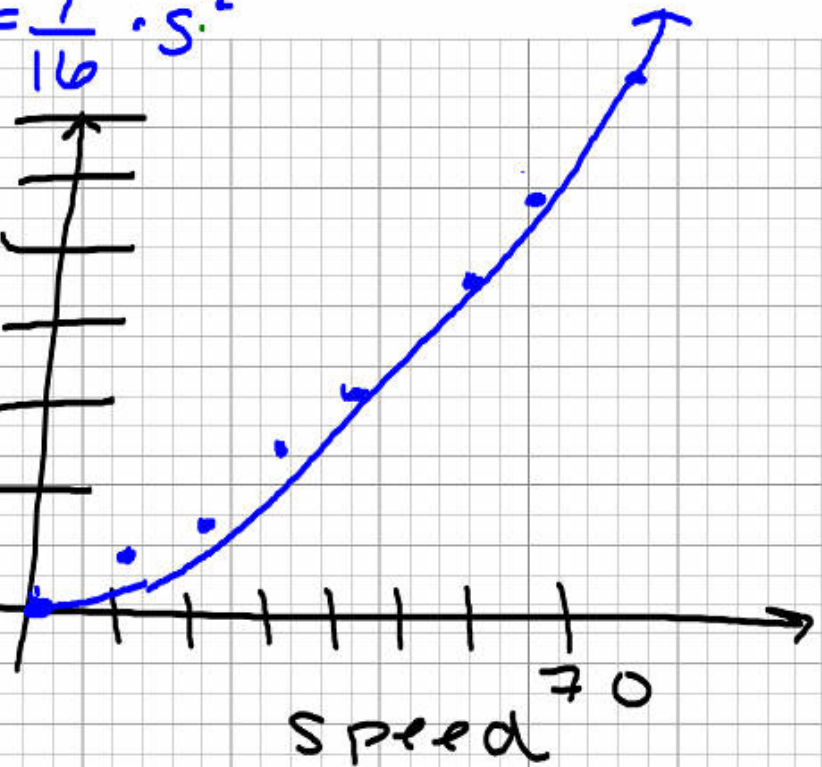
$$d = \frac{1}{16} \cdot s^2$$

Distance it takes a car to stop varies directly as the square of its speed.

$$d = \frac{1}{16} \cdot s^2$$

s	d
0	0
10	6.25
20	25
30	56.25
40	100
50	156.25
60	225
70	306.25

300
200
100

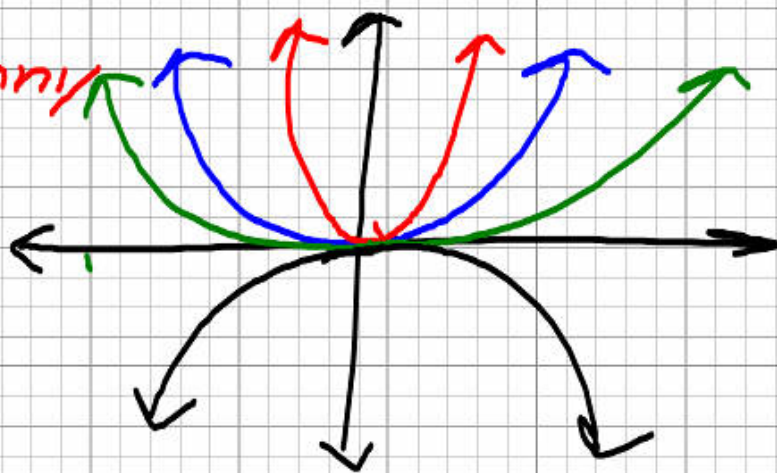


$$y = 1x^2$$

$$y = 2x^2 \rightarrow \text{skinnier}$$

$$y = \frac{1}{4}x^2$$

$$y = -1x^2$$



Properties of $y = kx^2$ $k > 0$
 $k < 0$

- * creates parabola ↪ ↩ ↪
- * each passes through origin $(0, 0)$
- * each parabola is reflection-symmetric
 - fold parabola in half over y -axis, everything matches up.
 - axis of symmetry

* Domain: \mathbb{R}

Range: $k > 0 \rightarrow \text{pos } \mathbb{R}, 0$
 $k < 0 \rightarrow \text{neg } \mathbb{R}, 0$

* $k > 0 \Rightarrow$ opens \uparrow ,
minimum
(vertex)

* $k < 0 \Rightarrow$ opens \downarrow ,
maximum
(vertex)

ex rate of change \Rightarrow slope

$(20, 25)$ $(40, 100)$

$$\frac{100 - 25}{40 - 20}$$

$$\frac{y_2 - y_1}{x_2 - x_1}$$

$$\frac{75}{20}$$

$y = 6x^2$
 $x = 2 \rightarrow x = 5$

x	y
2	1
5	1

$$\frac{15}{4} = \text{slope}$$